## **Claims**

[1]

1. A Ziegler-Natta catalyst for olefin polymerization, which is produced by a method comprising a step of reacting a transition metal compound having a general formula of MX  $_{p-(q+r)}$  (OAr  $_{1/q}$  (OAr  $_{2/r}$  , with an organomagnesium compound having a general formula of MgX  $_{2-m}$   $_{m}$  , wherein M represents a transition metal having an oxidation number of 4 or more, selected from Groups IV, V or VI of the Periodic table; X represents a halogen atom; Ar  $_{1/r}$  and Ar  $_{1/r}$  each represents substituted or unsubstituted aryl group of 6 to 30 carbon atoms, in which the Ar  $_{1/r}$  and Ar  $_{1/r}$  are not linked to each other; p represents the oxidation number of M of 4 or more; q and r satisfy  $0 \le q \le p$ ,  $0 \le r \le p$  and  $2 \le q+r \le p$ ; R represents an alkyl group of 1 to 16 carbon atoms; and m satisfies  $0 < m \le 2$ .

[2]

2. The Ziegler-Natta catalyst for olefin polymerization according to claim 1, wherein the transition metal compound and the organomagnesium compound are reacted at 60-90 °C with a molar ratio of  $0.1 \le$  the transition metal compound/the organomagnesium compound  $\le 0.5$ .

[3]

3. A method for olefin polymerization, which comprises carrying out polymerization in the presence of a main catalyst which is a Ziegler-Natta catalyst produced by a method comprising a step of reacting a transition metal compound having a general formula of MX (OAr) (OAr), with an organomagnesium compound having a general formula of MgX  $_{2-m}$   $_{m}$ , wherein M represents a transition metal having an oxidation number of 4 or more, selected from Groups IV, V or VI of the Periodic table; X represents a halogen atom; Ar and Ar each represents substituted or unsubstituted aryl group of 6 to 30 carbon atoms, in which the Ar and Ar are not linked to each other; p represents the oxidation number of M of 4 or more; q and r satisfy  $0 \le q \le p$ ,  $0 \le r \le p$  and  $2 \le q+r \le p$ ; R represents an alkyl group of 1 to 16 carbon atoms; and m satisfies  $0 < m \le 2$ , and

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a co-catalyst which is an alkyl aluminum compound having a general formula of AlR  $X_{n-(3-n)}$ , wherein R represents an alkyl group of 1 to 16 carbon atoms; X represents a halogen atom; and n satisfies  $1 \le n \le 3$ .

[4]

4. A method for olefin polymerization according to claim 3, wherein the alkyl aluminum compound is used with a molar ratio of  $0.5 \le$  the alkyl aluminum compound /the transition metal compound  $\le 500$ .